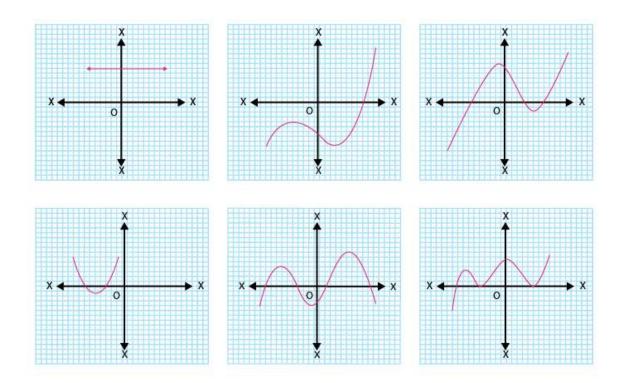
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CHAPTER 2 - POLYNOMIAL

Exercise 2.1 Page: 28

1. The graphs of y = p(x) are given in Fig. 2.10 below, for some polynomials p(x). Find the number of zeroes of p(x), in each case.



Solutions:

Graphical method to find zeroes:-

Total number of zeroes in any polynomial equation = total number of times the curve intersects xaxis.

- (i) In the given graph, the number of zeroes of p(x) is 0 because the graph is parallel to x-axis does not cut it at any point.
- (ii) In the given graph, the number of zeroes of p(x) is 1 because the graph intersects the x-axis at only one point.
- (iii) In the given graph, the number of zeroes of p(x) is 3 because the graph intersects the x-axis at any three points.

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(iv) In the given graph, the number of zeroes of p(x) is 2 because the graph intersects the x-axis at two points.

- (v) In the given graph, the number of zeroes of p(x) is 4 because the graph intersects the x-axis at four points.
- (vi) In the given graph, the number of zeroes of p(x) is 3 because the graph intersects the x-axis at three points.

Exercise 2.2 Page: 33

1. Find the zeroes of the following quadratic polynomials and verify the relationship between the zeroes and the coefficients.

Solutions:

(i)
$$x^2-2x-8$$

$$\Rightarrow$$
 x²-4x+2x-8 = x(x-4)+2(x-4) = (x-4)(x+2)

Therefore, zeroes of polynomial equation x^2-2x-8 are (4, -2)

Sum of zeroes = $4-2 = 2 = -(-2)/1 = -(Coefficient of x)/(Coefficient of x^2)$

Product of zeroes = $4 \times (-2) = -8 = -(8)/1 = (Constant term)/(Coefficient of x^2)$

(ii) $4s^2-4s+1$

$$\Rightarrow$$
4s²-2s-2s+1 = 2s(2s-1)-1(2s-1) = (2s-1)(2s-1)

Therefore, zeroes of polynomial equation $4s^2-4s+1$ are (1/2, 1/2)

Sum of zeroes = $(\frac{1}{2})+(\frac{1}{2})=1=-(-4)/4=-(Coefficient of s)/(Coefficient of s^2)$

Product of zeros = $(1/2) \times (1/2) = 1/4 = (Constant term)/(Coefficient of s^2)$

(iii) $6x^2-3-7x$

$$\Rightarrow 6x^2 - 7x - 3 = 6x^2 - 9x + 2x - 3 = 3x(2x - 3) + 1(2x - 3) = (3x + 1)(2x - 3)$$

Therefore, zeroes of polynomial equation $6x^2-3-7x$ are (-1/3, 3/2)

Sum of zeroes = $-(1/3)+(3/2) = (7/6) = -(Coefficient of x)/(Coefficient of x^2)$

Product of zeroes = $-(1/3)\times(3/2) = -(3/6) = (Constant term) / (Coefficient of x²)$

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(iv) $4u^2 + 8u$

$$\Rightarrow 4u(u+2)$$

Therefore, zeroes of polynomial equation $4u^2 + 8u$ are (0, -2).

Sum of zeroes = $0+(-2) = -2 = -(8/4) = -(Coefficient of u)/(Coefficient of u^2)$

Product of zeroes = $0 \times -2 = 0 = 0/4 = (Constant term)/(Coefficient of u^2)$

 $(v) t^2-15$

$$\Rightarrow$$
 t² = 15 or t = $\pm \sqrt{15}$

Therefore, zeroes of polynomial equation t^2 –15 are $(\sqrt{15}, -\sqrt{15})$

Sum of zeroes $=\sqrt{15}+(-\sqrt{15})=0=-(0/1)=-(Coefficient of t)/(Coefficient of t^2)$

Product of zeroes = $\sqrt{15} \times (-\sqrt{15}) = -15 = -15/1 = (Constant term) / (Coefficient of t²)$

(vi) $3x^2-x-4$

$$\Rightarrow 3x^2-4x+3x-4 = x(3x-4)+1(3x-4) = (3x-4)(x+1)$$

Therefore, zeroes of polynomial equation $3x^2 - x - 4$ are (4/3, -1)

Sum of zeroes = $(4/3)+(-1) = (1/3) = -(-1/3) = -(Coefficient of x) / (Coefficient of x^2)$

Product of zeroes= $(4/3)\times(-1) = (-4/3) = (Constant term) / (Coefficient of x²)$

- 2. Find a quadratic polynomial each with the given numbers as the sum and product of its zeroes, respectively.
- (i) 1/4,-1

Solution:

From the formulas of sum and product of zeroes, we know,

Sum of zeroes = $\alpha + \beta$

Product of zeroes = $\alpha \beta$

Sum of zeroes = $\alpha + \beta = 1/4$

Product of zeroes = $\alpha \beta = -1$

 \therefore If α and β are zeroes of any quadratic polynomial, then the quadratic polynomial equation can be written directly as:-

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$$x^2 - (\alpha + \beta)x + \alpha\beta = 0$$

$$x^2 - (1/4)x + (-1) = 0$$

$$4x^2-x-4=0$$

Thus, $4x^2-x-4$ is the quadratic polynomial.

(ii)
$$\sqrt{2}$$
, 1/3

Solution:

Sum of zeroes = $\alpha + \beta = \sqrt{2}$

Product of zeroes = $\alpha \beta = 1/3$

 \therefore If α and β are zeroes of any quadratic polynomial, then the quadratic polynomial equation can be written directly as:-

$$x^2-(\alpha+\beta)x + \alpha\beta = 0$$

$$x^2 - (\sqrt{2})x + (1/3) = 0$$

$$3x^2-3\sqrt{2}x+1=0$$

ins: Noyaleducation.org Thus, $3x^2-3\sqrt{2}x+1$ is the quadratic polynomial.

(iii)
$$0, \sqrt{5}$$

Solution:

Given,

Sum of zeroes = $\alpha + \beta = 0$

Product of zeroes = $\alpha \beta = \sqrt{5}$

 \therefore If α and β are zeroes of any quadratic polynomial, then the quadratic polynomial equation can be written directly

as:-

$$x^2 - (\alpha + \beta)x + \alpha\beta = 0$$

$$x^2-(0)x+\sqrt{5}=0$$

Thus, $x^2 + \sqrt{5}$ is the quadratic polynomial.

(iv) 1, 1

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Solution:

Given,

Sum of zeroes = $\alpha + \beta = 1$

Product of zeroes = $\alpha \beta = 1$

 \therefore If α and β are zeroes of any quadratic polynomial, then the quadratic polynomial equation can be written directly as:-

$$x^2 - (\alpha + \beta)x + \alpha\beta = 0$$

$$x^2-x+1=0$$

Thus, x^2-x+1 is the quadratic polynomial.

Solution:

Given,

Sum of zeroes = $\alpha + \beta = -1/4$

Product of zeroes = $\alpha \beta = 1/4$

 \therefore If α and β are zeroes of any quadratic polynomial, then the quadratic polynomial equation can be written directly as:-

$$x^2 - (\alpha + \beta)x + \alpha\beta = 0$$

$$x^2 - (-1/4)x + (1/4) = 0$$

$$4x^2 + x + 1 = 0$$

Thus, $4x^2+x+1$ is the quadratic polynomial.

Solution:

Given,

Sum of zeroes = $\alpha + \beta = 4$

Product of zeroes = $\alpha\beta = 1$

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 \therefore If α and β are zeroes of any quadratic polynomial, then the quadratic polynomial equation can be written directly as:-

$$x^2-(\alpha+\beta)x+\alpha\beta=0$$

$$x^2-4x+1=0$$

Thus, x^2-4x+1 is the quadratic polynomial.

Exercise 2.3 Page: 36

1. Divide the polynomial p(x) by the polynomial g(x) and find the quotient and remainder in each of the following:

(i)
$$p(x) = x^3-3x^2+5x-3$$
, $g(x) = x^2-2$

Solution:

Given,

Dividend =
$$p(x) = x^3-3x^2+5x-3$$

Divisor =
$$g(x) = x^2 - 2$$

Therefore, upon division we get,

Quotient =
$$x-3$$

Remainder =
$$7x-9$$

(ii)
$$p(x) = x^4-3x^2+4x+5$$
, $g(x) = x^2+1-x$

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Solution:

Given,

Dividend =
$$p(x) = x^4 - 3x^2 + 4x + 5$$

Divisor =
$$g(x) = x^2 + 1-x$$

$$x^{2} - x + 1$$

$$x^{2} + x - 3$$

$$x^{2} - x + 1$$

$$x^{2} + x - 3$$

$$x^{4} + 0x^{3} - 3x^{2} + 4x + 5$$

$$x^{3} - 4x^{2} + 4x + 5$$

$$x^{3} - 4x^{2} + 4x + 5$$

$$x^{3} - x^{2} + x$$

$$x^{3} - x^{2} + x$$

$$x^{3} - x^{2} + x$$

$$x^{3} - 3x^{2} + 3x + 5$$

$$x^{3} - 3x^{2} + 3x + 5$$

$$x^{3} - 3x^{2} + 3x - 3$$

$$x^{3} - 3x^{2$$

Therefore, upon division we get,

Quotient =
$$x^2 + x - 3$$

$$Remainder = 8$$

(iii)
$$p(x) = x^4 - 5x + 6$$
, $g(x) = 2 - x^2$

Solution:

Given,

Dividend =
$$p(x) = x^4 - 5x + 6 = x^4 + 0x^2 - 5x + 6$$

Divisor =
$$g(x) = 2-x^2 = -x^2+2$$

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 $+0x^3 +0x^2 -5x +6$

Therefore, upon division we get,

Quotient = $-x^2-2$

Remainder = -5x + 10

ttps://loyaleducation. 2. Check whether the first polynomial is a factor of the second polynomial by dividing the second polynomial by the first polynomial:

(i)
$$t^2$$
-3, $2t^4$ + $3t^3$ -2 t^2 -9 t -12

Solutions:

Given,

First polynomial $= t^2-3$

Second polynomial = $2t^4 + 3t^3 - 2t^2 - 9t - 12$

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https://oyaledneation.org As we can see, the remainder is left as 0. Therefore, we say that, t^2 -3 is a factor of $2t^4 + 3t^3 - 2t^2 - 9t$ 12.

(ii) x^2+3x+1 , $3x^4+5x^3-7x^2+2x+2$

Solutions:

Given,

First polynomial = x^2+3x+1

Second polynomial = $3x^4+5x^3-7x^2+2x+2$

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Silloyalednication. As we can see, the remainder is left as 0. Therefore, we say that, $x^2 + 3x + 1$ is a factor of $3x^4 + 5x^3$ - $7x^2+2x+2$.

(iii)
$$x^3-3x+1$$
, $x^5-4x^3+x^2+3x+1$

Solutions:

Given.

First polynomial = x^3-3x+1

Second polynomial = $x^5-4x^3+x^2+3x+1$

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As we can see, the remainder is not equal to 0. Therefore, we say that, x^3-3x+1 is not a factor of $x^5-4x^3+x^2+3x+1$.

3. Obtain all other zeroes of $3x^4+6x^3-2x^2-10x-5$, if two of its zeroes are $\sqrt{(5/3)}$ and $-\sqrt{(5/3)}$.

Solutions:

Since this is a polynomial equation of degree 4, hence there will be total 4 roots.

 $\sqrt{(5/3)}$ and $-\sqrt{(5/3)}$ are zeroes of polynomial f(x).

$$\therefore (x - \sqrt{5/3})) (x + \sqrt{5/3}) = x^2 - (5/3) = 0$$

 $(3x^2-5)=0$, is a factor of given polynomial f(x).

Now, when we will divide f(x) by $(3x^2-5)$ the quotient obtained will also be a factor of f(x) and the remainder will be 0.

$$x^{2} + 2x + 1$$

$$3x^{2} - 5 \overline{\smash)3x^{4} + 6x^{3} - 2x^{2} - 10x - 5}$$

$$3x^{4} - 5x^{2}$$

$$(\cdot) \qquad (+)$$

$$+ 6x^{3} + 3x^{2} - 10x - 5$$

$$- 6x^{3} - 10x$$

$$(+) \qquad (\cdot)$$

$$3x^{2} - 5$$

$$3x^{2} - 5$$

$$(\cdot) \qquad (+)$$

$$0$$

Therefore, $3x^4 + 6x^3 - 2x^2 - 10x - 5 = (3x^2 - 5)(x^2 + 2x + 1)$

Now, on further factorizing (x^2+2x+1) we get,

$$x^2+2x+1 = x^2+x+x+1 = 0$$

$$x(x+1)+1(x+1) = 0$$

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$$(x+1)(x+1) = 0$$

So, its zeroes are given by: x = -1 and x = -1.

Therefore, all four zeroes of given polynomial equation are:

$$\sqrt{(5/3)}$$
, $\sqrt{(5/3)}$, -1 and -1 .

Hence, is the answer.

4. On dividing x^3-3x^2+x+2 by a polynomial g(x), the quotient and remainder were x-2 and -2x+4, respectively. Find g(x).

Solution:

Given,

Dividend,
$$p(x) = x^3 - 3x^2 + x + 2$$

Quotient =
$$x-2$$

Remainder =
$$-2x+4$$

We have to find the value of Divisor,
$$g(x) = ?$$

As we know,

$$Dividend = Divisor \times Quotient + Remainder$$

$$\therefore x^3 - 3x^2 + x + 2 = g(x) \times (x - 2) + (-2x + 4)$$

$$x^3-3x^2+x+2-(-2x+4) = g(x)\times(x-2)$$

Therefore,
$$g(x) \times (x-2) = x^3-3x^2+3x-2$$

Now, for finding
$$g(x)$$
 we will divide x^3-3x^2+3x-2 with $(x-2)$

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Therefore, $g(x) = (x^2-x+1)$

5. Give examples of polynomials p(x), g(x), q(x) and r(x), which satisfy the division algorithm and aleducation.0

(i) $\deg p(x) = \deg q(x)$

(ii) $\deg q(x) = \deg r(x)$

(iii) deg r(x) = 0

Solutions:

According to the division algorithm, dividend p(x) and divisor g(x) are two polynomials, where $g(x) \neq 0$. Then we can find the value of quotient q(x) and remainder r(x), with the help of below given formula;

 $Dividend = Divisor \times Quotient + Remainder$

$$\therefore p(x) = g(x) \times q(x) + r(x)$$

Where r(x) = 0 or degree of r(x) < degree of g(x).

Now let us proof the three given cases as per division algorithm by taking examples for each.

(i) $\deg p(x) = \deg q(x)$

Degree of dividend is equal to degree of quotient, only when the divisor is a constant term.

Let us take an example, $p(x) = 3x^2 + 3x + 3$ is a polynomial to be divided by g(x) = 3.

So, $(3x^2+3x+3)/3 = x^2+x+1 = q(x)$

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Thus, you can see, the degree of quotient q(x) = 2, which also equal to the degree of dividend p(x).

Hence, division algorithm is satisfied here.

(ii)
$$\deg q(x) = \deg r(x)$$

Let us take an example, $p(x) = x^2 + 3$ is a polynomial to be divided by g(x) = x - 1.

So,
$$x^2 + 3 = (x - 1) \times (x) + (x + 3)$$

Hence, quotient q(x) = x

Also, remainder r(x) = x + 3

Thus, you can see, the degree of quotient q(x) = 1, which is also equal to the degree of remainder r(x).

Hence, division algorithm is satisfied here.

(iii)
$$deg r(x) = 0$$

The degree of remainder is 0 only when the remainder left after division algorithm is constant.

s://loyaleducati Let us take an example, $p(x) = x^2 + 1$ is a polynomial to be divided by g(x) = x.

So,
$$x^2 + 1 = (x) \times (x) + 1$$

Hence, quotient q(x) = x

And, remainder r(x) = 1

Clearly, the degree of remainder here is 0.

Hence, division algorithm is satisfied here.

Exercise 2.4 Page: 36

1. Verify that the numbers given alongside of the cubic polynomials below are their zeroes. Also verify the relationship between the zeroes and the coefficients in each case:

(i)
$$2x^3+x^2-5x+2$$
; $-1/2$, 1, -2

Solution:

Given,
$$p(x) = 2x^3 + x^2 - 5x + 2$$

And zeroes for p(x) are = 1/2, 1, -2

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 $\therefore p(1/2) = 2(1/2)^3 + (1/2)^2 - 5(1/2) + 2 = (1/4) + (1/4) - (5/2) + 2 = 0$

$$p(1) = 2(1)^3 + (1)^2 - 5(1) + 2 = 0$$

$$p(-2) = 2(-2)^3 + (-2)^2 - 5(-2) + 2 = 0$$

Hence, proved 1/2, 1, -2 are the zeroes of $2x^3+x^2-5x+2$.

Now, comparing the given polynomial with general expression, we get;

$$ax^3+bx^2+cx+d=2x^3+x^2-5x+2$$

$$a=2$$
, $b=1$, $c=-5$ and $d=2$

As we know, if α , β , γ are the zeroes of the cubic polynomial ax^3+bx^2+cx+d , then;

$$\alpha + \beta + \gamma = -b/a$$

$$\alpha\beta + \beta\gamma + \gamma\alpha = c/a$$

$$\alpha \beta \gamma = - d/a$$
.

Therefore, putting the values of zeroes of the polynomial,

$$\alpha + \beta + \gamma = \frac{1}{2} + 1 + (-2) = -\frac{1}{2} = -\frac{b}{a}$$

$$\alpha\beta + \beta\gamma + \gamma\alpha = (1/2 \times 1) + (1 \times -2) + (-2 \times 1/2) = -5/2 = c/a$$

$$\alpha \beta \gamma = \frac{1}{2} \times 1 \times (-2) = -\frac{2}{2} = -\frac{d}{a}$$

Hence, the relationship between the zeroes and the coefficients are satisfied.

(ii)
$$x^3-4x^2+5x-2$$
; 2, 1, 1

Solution:

Given,
$$p(x) = x^3-4x^2+5x-2$$

And zeroes for p(x) are 2,1,1.

$$p(2) = 2^{3}-4(2)^{2}+5(2)-2 = 0$$

$$p(1) = 1^3 - (4 \times 1^2) + (5 \times 1) - 2 = 0$$

Hence proved, 2, 1, 1 are the zeroes of x^3-4x^2+5x-2

Now, comparing the given polynomial with general expression, we get;

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$$\therefore ax^3+bx^2+cx+d = x^3-4x^2+5x-2$$

$$a = 1$$
, $b = -4$, $c = 5$ and $d = -2$

As we know, if α , β , γ are the zeroes of the cubic polynomial ax^3+bx^2+cx+d , then;

$$\alpha + \beta + \gamma = -b/a$$

$$\alpha\beta + \beta\gamma + \gamma\alpha = c/a$$

$$\alpha \beta \gamma = -d/a$$
.

Therefore, putting the values of zeroes of the polynomial,

$$\alpha + \beta + \gamma = 2 + 1 + 1 = 4 = -(-4)/1 = -b/a$$

$$\alpha\beta + \beta\gamma + \gamma\alpha = 2 \times 1 + 1 \times 1 + 1 \times 2 = 5 = 5/1 = c/a$$

$$\alpha\beta\gamma = 2 \times 1 \times 1 = 2 = -(-2)/1 = -d/a$$

Hence, the relationship between the zeroes and the coefficients are satisfied.

2. Find a cubic polynomial with the sum, sum of the product of its zeroes taken two at a time, and the product of its zeroes as 2, -7, -14 respectively.

Solution:

Let us consider the cubic polynomial is ax^3+bx^2+cx+d and the values of the zeroes of the MPS://loya polynomials be α , β , γ .

As per the given question,

$$\alpha + \beta + \gamma = -b/a = 2/1$$

$$\alpha\beta + \beta\gamma + \gamma\alpha = c/a = -7/1$$

$$\alpha \beta \gamma = -d/a = -14/1$$

Thus, from above three expressions we get the values of coefficient of polynomial.

$$a = 1$$
, $b = -2$, $c = -7$, $d = 14$

Hence, the cubic polynomial is $x^3-2x^2-7x+14$

3. If the zeroes of the polynomial x^3-3x^2+x+1 are a-b, a, a+b, find a and b.

Solution:

We are given with the polynomial here,

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$$p(x) = x^3 - 3x^2 + x + 1$$

And zeroes are given as a - b, a, a + b

Now, comparing the given polynomial with general expression, we get;

$$px^3+qx^2+rx+s = x^3-3x^2+x+1$$

$$p = 1$$
, $q = -3$, $r = 1$ and $s = 1$

Sum of zeroes = a - b + a + a + b

$$-q/p = 3a$$

Putting the values q and p.

$$-(-3)/1 = 3a$$

$$a=1$$

Thus, the zeroes are 1-b, 1, 1+b.

Now, product of zeroes = 1(1-b)(1+b)

$$-s/p = 1-b^2$$

$$-1/1 = 1-b^2$$

$$b^2 = 1 + 1 = 2$$

$$b = \pm \sqrt{2}$$

Hence, $1-\sqrt{2}$, 1, $1+\sqrt{2}$ are the zeroes of x^3-3x^2+x+1 .

4. If two zeroes of the polynomial x^4 - $6x^3$ - $26x^2$ +138x-35 are $2 \pm \sqrt{3}$, find other zeroes.

Solution:

Since this is a polynomial equation of degree 4, hence there will be total 4 roots.

Let
$$f(x) = x^4-6x^3-26x^2+138x-35$$

Since $2 + \sqrt{3}$ and $2 - \sqrt{3}$ are zeroes of given polynomial f(x).

$$\therefore [x-(2+\sqrt{3})][x-(2-\sqrt{3})]=0$$

$$(x-2-\sqrt{3})(x-2+\sqrt{3})=0$$

On multiplying the above equation we get,

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 x^2-4x+1 , this is a factor of a given polynomial f(x).

Now, if we will divide f(x) by g(x), the quotient will also be a factor of f(x) and the remainder will be 0.

$$x^{2}-2x-35$$

$$x^{2}-4x+1$$

$$x^{4}-6x^{3}-26x^{2}+138x-35$$

$$-2x^{3}+8x^{2}-2x$$

$$x^{4}-6x^{3}-27x^{2}+138x-35$$

$$-2x^{3}+8x^{2}-2x$$

$$x^{4}-6x^{3}-26x^{2}+140x-35$$

$$-35x^{2}+140x-35$$

$$x^{4}-6x^{3}-26x^{2}+138x-35=(x^{2}-4x+1)(x^{2}-2x-35)$$

$$x^{4}-6x^{3}-26x^{2}+138x-35=(x^{2}-4x+1)(x^{2}-2x-35)$$

$$x^{4}-6x^{3}-26x^{2}+138x-35=(x^{2}-4x+1)(x^{2}-2x-35)$$

$$x^{4}-6x^{3}-26x^{2}+138x-35=0$$

$$x^{4}-6x^{3$$

So,
$$x^4-6x^3-26x^2+138x-35 = (x^2-4x+1)(x^2-2x-35)$$

Now, on further factorizing $(x^2-2x-35)$ we get,

$$x^2-(7-5)x-35 = x^2-7x+5x+35 = 0$$

$$x(x-7) + 5(x-7) = 0$$

$$(x+5)(x-7) = 0$$

So, its zeroes are given by:

$$x = -5$$
 and $x = 7$.

Therefore, all four zeroes of given polynomial equation are: $2+\sqrt{3}$, $2-\sqrt{3}$, -5 and 7.

0.5: If the polynomial $x^4 - 6x^3 + 16x^2 - 25x + 10$ is divided by another polynomial $x^2 - 2x + k$, the remainder comes out to be x + a, find k and a.

Solution:

Let's divide $x^4 - 6x^3 + 16x^2 - 25x + 10$ by $x^2 - 2x + k$.

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(4k-25+16-2k)x+[10-k(8-k)]

iths: Novaleducation.org Given that the remainder of the polynomial division is x + a.

$$(4k - 25 + 16 - 2k)x + [10 - k(8 - k)] = x + a$$

$$(2k-9)x + (10-8k+k^2) = x + a$$

Comparing the coefficients of the above equation, we get;

$$2k - 9 = 1$$

$$2k = 9 + 1 = 10$$

$$k = 10/2 = 5$$

And

$$10 - 8k + k^2 = a$$

$$10 - 8(5) + (5)^2 = a$$
 [since k = 5]

$$10 - 40 + 25 = a$$

$$a = -5$$

Therefore, k = 5 and a = -5.